Mathematica code for least-squares cone fitting and equal-area stereonet representation

Kieran F. Mulchrone a, Daniel Pastor-Galán b,*, Gabriel Gutiérrez-Alonso b

a Department of Applied Mathematics, University College, Cork, Ireland
b Departamento de Geología, Universidad de Salamanca, 37008 Salamanca, Spain

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ABSTRACT

In structural geology it is often assumed that folds are cylindrical. However, most structures are conical to some degree. Due to the lack of software capable of accurately estimating the best fit cone from a set of oriented data, we developed a Mathematica application capable of (1) plotting oriented data (lines and planes) on an equal area stereonet, (2) calculating the orientation matrix, the distribution shape and intensity parameters, (3) plotting the eigenvectors and (4) estimating and plotting the best fit cone, a small circle. We present both synthetic and natural data demonstrating its robustness and accuracy calculating the best fit cone.

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1. Introduction

Folds are cylindrical, most of them have, to a certain degree, a conical shape (Fig. 1). However, to our knowledge, the most popular free available stereographic applications such as Stereonet (Cardozo and Allmendinger, 2013; Allmendinger et al., 2012), Georient (Holcombe software), Openstereo (Grohmann and Campanha, 2010) or Stere32 (Röller and Trepmann, 2008) or other Stereonet Mathematica applications – see Mathematica for Geology (Hanebergs) and Geological Program (Mookerjee) – either do not provide best fit cone functionality or provide methods which fail to estimate the best fit cone when dealing with complex distributions. In this paper we present Mathematica code which provides a robust cone fitting algorithm with the motivation of filling the gap found in other stereographic projection software.

A conical surface is the result of rotating an oblique line (the generator) around a defined rotation axis. In geology, geometrically, a conical fold is characterized by the trend and plunge of its axis and by the angle between the generatrix of the conical surface and the fold axis, also known as semiapical angle (\(\alpha/2\)) (Wilson, 1967; Pueyo et al., 2003). Perfect cylindrical folds can be considered as a special case of a conical fold; then have \(\alpha/2\) equal to 0°. Identification and analysis of conical folds in nature are conducted using stereographic projection of geologic surfaces, typically bedding (\(\pi\)-diagrams) which, when truly representative of a conical surface, scatter along a small circle on the stereonet. When the geometry of the studied fold is more complicated, such as in elliptical conical folds or complex non-cylindrical folds, the \(\pi\)-diagram scatters along ellipses or irregular paths. Ramsay (1967 p. 349) indicated that conical folds are rare in nature, and (Ramsay and Huber, 1987, p. 311) suggested that the geometry of natural surfaces is probably more complex than a simple conical which is probably a more accurate assessment of the situation at most scales. Nevertheless, conical folding is often a valid approximation for non-cylindrical folds at suitably chosen scales and complex folded surfaces can be easily treated as several different conical surfaces.

Structural geologists have shown interest in conical folding trying to solve the problem of reconstructing bedding-parallel sedimentary lineation orientations (Cummins, 1966; Wilson, 1967; Ramsay, 1967 pp. 496–498) and, more recently, the problem of how to restore paleomagnetic data directions (Pueyo et al., 2003; Weil et al., 2013) or the location of mineralizations (Keppie et al., 2002) or hydrocarbon reservoir rocks (Mandujano and Keppie, 2006). The most frequently described conical geometry in rocks is the lateral terminations of cylindrical folds (e.g. Webb and Lawrence, 1986). The geometry is related to the propagation of folds during which both the interlimb tightening and fold axis lengthening occur. Moreover, conical folds can also form by fold interference (Ramsay, 1962; Wilson, 1967; Pastor-Galán et al., 2012a), or by folds forming in shear zones.
been proven to provide accurate solutions to different cases of
This method is robust to apply to non-symmetrical data and has
the improved least-squares algorithm of Gray et al. (1980).
algorithm presented by (Fisher et al., 1987, p. 140–143) that is
2008). We propose using an implementation of the iterative
based on the method of Mardia and Gadsden (1977) and
ments to a small circle and to quantify the suitability of the
terminate along their axial trend.
Mathematical methods have been developed to fit measure-
ments to a small circle and to quantify the suitability of the
calculation fit (e.g. Ramsay, 1967; Fisher et al., 1987).
approaches to fitting planar data to a cone typically involve least squares
minimisation of a function involving the direction cosines of poles
to planes (Ramsay, 1967; Venkitasubramanyan, 1971; Cruden and
Charlesworth, 1972), and provide estimates for the orientation of
the cone axis and the semi-apical angle. Problems associated with
these initial methods were resolved by minimising the squares of the
actual angular deviations (Kelker and Langenberg, 1982;
Fisher et al., 1987) by making the minimisation problem
non-linear and requiring iterative techniques to determine a
solution. The problem may also be solved using the least eigenvector of the orientation matrix (Fisher et al., 1987, p. 33), though
this approach only works for symmetrical datasets with a semi-
apical angle less than 45°. Bingham's distribution on a sphere can
also be used to find the best-fit great circle to fold data forming a
pair of clusters which is often the case for geological data (Kelker and Langenberg, 1976). Subsequently, using a transformation to
spherical coordinates (Stockmal and Spang, 1982), a least-squares
best fit was identified for the simulated data of Cruden and
Charlesworth (1972). Methods able to cope with elliptical conical
folds and statistical tests for distinguishing between circular and
elliptical data have also been developed (Kelker and Langenberg,
1987, 1988). Non-geologists' statisticians have also shown an
interest in this problem (Mardia and Gadsden, 1977; Rivest,
2008). We propose using an implementation of the iterative
algorithm presented by (Fisher et al., 1987, p. 140–143) that is
based on the method of Mardia and Gadsden (1977) and
the improved least-squares algorithm of Gray et al. (1980).
This method is robust to apply to non-symmetrical data and has
been proven to provide accurate solutions to different cases of
(real, as is the data used in this paper, and simulated conical folds.
It works for non-symmetrical data and apical angles greater than
45°).

2. Code description and algorithms

The primary motivation for developing the code was to
provide a robust cone fitting algorithm which was lacking in
tested available software. Necessary additional functionality
includes a collection of useful methods for analysis of orientation
data typically collected by structural geologists. In this section a
brief discussion and description of the data formats, analyses and
graphical outputs are provided.

2.1. Plotting data

As far as the authors are aware, there is no internationally
recognized standard for digital storage of oriented geological data.
For this application data is stored in a text comma separated
variable (csv) file format that can be readily imported into
Mathematica and easily created in common spreadsheet packages
such as Microsoft Excel, OpenOffice, etc. The file must conform to
the following format: The first column contains either L (for linear
data) or P (for planar data). If the data are planes then the next
two columns contain either the strike and dip (using the right
hand rule, Groshong, 2008, pp. 41–43; Ragan, 2009, p. 4) or dip
direction and dip respectively. If the data are lines then the next
two columns contain the trend and plunge respectively. The final
and fourth column is reserved for categorization of data. Fig. 2
shows part of the contents of a data input file in Excel.

Once a file has been created it may be imported into Mathe-
matica using the Import command. For convenience we provide a
method, ImportSG, that simplifies the process. ImportSG takes
two arguments: the first specifies the file to be imported and the
second specifies the format used for planar data which may be
either “RHR” (i.e. right hand rule strike and dip) or “DDD” (i.e. dip
direction and dip data). ImportSG imports the data and separates
it into subsets based on data type and category and also converts
the orientation data into triplets of direction cosines, the format
used in analysis and plotting routines. The data is subdivided into
groups on the basis of whether it is planar of linear and also the
category. For each unique combination of data-type and category
a new group is created. This approach is unrestricted but care
needs to be taken when creating input files so that the resulting
data is not too complex. It may be convenient to store files related
to a single project in a single directory and rather than having to

Fig. 2. Example format of data in excel. First column specifies if the data are
planar or linear and the second column is the strike, dip direction or trend
spending on the format. The third column specifies the dip or plunge and the final
column is a category for analysis of complex datasets.
specify the full path to a file. The standard SetDirectory command can be used to select a particular directory for use.

The method EqualAreaPlot creates equal-area stereonets and has four arguments. The first argument is the data to be plotted and ought to be the output from ImportSG. The second argument specifies the size of the symbols on the stereonet and defaults to a value of 0.02. The third argument controls the colour and shape of the symbols used for each dataset in the data. For full control, a colour/shape combination for each dataset can be specified, otherwise, suitable values are randomly generated. The following shapes are provided: "Circle", an open circle, "FCircle", a filled circle, "OCircle", a filled circle with a black outline and similarly defined "Square", "FSquare", "OSquare". The final argument is either True or False and specifies whether or not a legend is displayed. The text of the legend is composed from the category and type of data. For example if the type is "L" and the category is "F1" then the legend is "F1 (L)". Example code: Click here to enter text.

```mathematica
(* select the directory with the data *)
SetDirectory["C:\Users\km\Dropbox\research\papers\Conical Folding Mathematica\Data"]

(* import data from csv file *)
data = ImportSG["inner_anticline.csv"];

(* create a plot of the data *)
EqualAreaPlot[data, 0.02, {Purple,"Square"}, True]
```

The resulting plot is shown in Fig. 3. The code is fairly flexible and allows for a reasonable level of control to the user.

For less sophisticated data analysis, another more general SimpleEqualAreaPlot method is provided which takes four arguments. The first is a list of either strikes and dips or trends and plunges, the second specifies the type of data (either "P" or "L" respectively), the third determines the size of the symbol and the final argument specifies the type in the same way as for EqualAreaPlot above. Example code: Click here to enter text.

```
(* select the directory with the data *)
SetDirectory["C:\Users\km\Dropbox\research\papers\Conical Folding Mathematica\Data"]

(* import data from csv file *)
data = ImportSG["inner_anticline.csv"]; (* import data from csv file *)

(* create a plot of the data *)
EqualAreaPlot[data, 0.02, {{Purple,"Square"},[Blue,"OCircle"], [Green,"OSquare"],[Red,"OCircle"]}, True]
```

Fig. 3. An example stereonet of planar data categorized as either normal or overturned.

(* plot the data *)
SimpleEqualAreaPlot[data, "P", 0.02, {Black,"FCircle"}]

2.2. Orientation matrix and distribution classification

As it is standard practice in the analysis of oriented data the eigenvalues and eigenvectors of the orientation matrix provide a good summary of oriented data and permit classification. The orientation matrix is calculated by pre-multiplying the matrix of direction cosines by its transpose (Fisher et al., 1987, p. 33). Given a set of direction cosines data the orientation matrix is

\[
T = \begin{pmatrix}
\sum x_i^2 & \sum x_i y_i & \sum x_i z_i \\
\sum y_i x_i & \sum y_i^2 & \sum y_i z_i \\
\sum z_i x_i & \sum z_i y_i & \sum z_i^2
\end{pmatrix}
\]

The eigenvalues and corresponding eigenvectors of \( T \) are denoted by \( t_1, t_2, t_3 \) and \( u_1, u_2, u_3 \) respectively where \( 0 \leq t_1 \leq t_2 \leq t_3 \). If the normalized eigenvalues of the orientation matrix are given by \( t_1 = t_1/n \) etc. then the shape of the distribution is described by

\[
\gamma = \frac{\log(t_3/t_2)}{\log(t_2/t_1)}
\]

where \( \gamma \) close to 0 is a girdle distribution and \( \gamma \) near 1 is mixed and \( \gamma > 1 \) is a uniaxial cluster distribution. The strength or intensity of the distribution is described by

\[
zeta = \log(t_3/t_1)
\]

where values close to 0 indicate weak distributions and strong distributions occur for \( zeta \) greater than around 3

In the case of a uniaxial distribution \( t_3 \) is considerably larger than the other two eigenvalues and the eigenvector \( u_3 \) provides a good estimate of the average orientation. In the case of a girdle distribution \( t_2 \) and \( t_3 \) are larger than \( t_1 \) and \( u_1 \) is a good estimate for the pole to the best fit great circle.

For convenience a method named AnalyseSGData is provided which takes a single dataset returned from ImportSG as its first argument and the second argument is either "T" for text output or "G" for graphical output. Further arguments control the graphical output. The third argument controls the symbol used for data, the fourth argument controls the eigenvector symbol and the final argument specifies the colour of the great circle arcs. Text output consists of the normalized eigenvalues, the trend and plunge of the eigenvectors, the shape and strength parameters. Example code: Click here to enter text.

```
(* analyse each dataset separately and get textual output *)
AnalyseSGData[data[1],"T"]

{{0.00249152,0.0348249,0.962684},{308.671,11.1581},{92.3696,16.2737}},1.25856,5.95683

AnalyseSGData[data[2],"T"]

{{0.0618874,0.453435,0.484678},{20.4175,22.6605},{149.174,56.3001}},0.0334578,2.05817

(* generate graphical output *)
```
AnalyseSGData[ data[1], "G", {Black, "Square"}, {Black, "OCircle"}, Black]
AnalyseSGData[ data[2], "G", {Black, "Square"}, {Black, "OCircle"}, Black]

The associated graphical output is shown in Fig. 4. The eigenvectors are marked on the resulting plot and labelled by their corresponding eigenvalue (to).

2.3. Fitting a cone

The method implemented for fitting a cone is that of Fisher et al. (1987) pp. 140-143, which is based on Mardia and Gadsden (1977) and seeks to minimize the angular distance between points distributed on the sphere and a small circle, i.e. the cone. Let the cone axis have direction cosines \( \lambda=(\lambda, \mu, \nu) \) and angular distance from a point on the cone to the axis is \( \psi \). The equation of directions/points \((x,y,z)\) on the cone is

\[
x\lambda + y\mu + z\nu = \cos \psi
\]

Let the \( j \)th estimate of \( \lambda \) be \( \lambda_j \) and that of \( \psi \) be \( \psi_j \). The iterative algorithm proceeds as follows:

1. Take \( u_3 \) to be an initial guess for \( (\lambda, \mu, \nu) \), i.e. \( \lambda_0 = u_3 \).
2. Calculate \( \psi_j \) from

\[
\tan \psi_j = \frac{\sum_{i=1}^{n} \sqrt{1-(X_i\lambda_j-1)^2}}{\sum_{i=1}^{n} X_i\lambda_j-1}
\]

3. Calculate the following vectors:

\[
X_i = \frac{(X_i\lambda_j-1)X_i - \lambda_j -1}{\sqrt{1-(X_i\lambda_j-1)^2}} \quad i = 1n
\]

\[
Y = \cos \psi_j \sum_{i=1}^{n} X_i - \sin \psi_j \sum_{i=1}^{n} X_i
\]

\[
\lambda_j = \frac{Y}{\sqrt{YY}}
\]

4. Repeat steps 2 and 3 until the difference between the current and previous estimates for \( \lambda \) and \( \psi \) is acceptably small.

The algorithm works well when all the target data occupies a single hemisphere but may fail otherwise. This is fixed by applying a rotation to the data such that the first eigenvector \( (u_3) \) is rotated into parallelism with the \( z \)-axis. The analysis is then

Fig. 4. (a) Eigen analysis of cluster data, note that the eigenvector corresponding to the largest eigenvalue \( (u_3) \) parallels the average direction. (b) In this case the eigenvector corresponding to the lowest eigenvalue parallels the pole to the best fit great circle.

Fig. 5. Best fit cones using the algorithm described.
carried out as described above except that the fitted cone axis is rotated back to the correct orientation.

The algorithm works well when the apical angle is less than approximately 45. For larger apical angles the algorithm may fail. This is due to exclusively using the third eigenvector as an initial guess for the cone axis. If the apical angle is less than 45° then \( \mathbf{u}_3 \) takes an orientation close to the cone axis. On the other hand if the apical axis is greater than 45° then it may be one of the other eigenvectors which is close to the cone axis and should be used as an initial guess. Thus a parameter is provided which allows the user to specify the eigenvector to use as an initial guess. The AnalyseSGData method of the previous section allows visual inspection to deduce the correct initial eigenvector to be selected (see Section 2.4 for examples).

Cone fitting is facilitated by the method FitConeSG which takes a single dataset returned from ImportSG as its first argument and the second argument is either “T” for text output or “G” for vectorial graphical output. The third argument controls the symbol used for data, the fourth argument controls the cone axis symbol and the fifth argument specifies the colour of the cone curve. The final argument specifies the number of data to generate. The method works by generating a unit vector \( \mathbf{v} \) randomly oriented in the \( xy \)-plane and then rotating a unit vector parallel to the \( z \)-axis around \( \mathbf{v} \) by an angle selected from a normal distribution with mean equal to the apical angle and the specified standard deviation. Finally the cone is rotated in parallel with the desired cone axis.

To analyse the data produced by GenSGData it is necessary to place it in a csv file confirming to the format specified earlier. This process is simplified by the ExportSGData method which takes as its first argument the trend/plunge data generated by GenSGData, the second argument is the name of the csv file and the last argument is the category.

Two example datasets presented in Fig. 6 indicate the robustness of the method and code.

\[
\text{Example 1 (see Fig. 6a and b):}
\]

\[
\text{(* generate data with cone axis trending 054 and plunging 60, apical angle 70, standard deviation of 5 and 50 points *)}
\]

\[
\text{dataset} = \text{GenSGData}[[54, 60], 70, 5, 50];
\]

\[
\text{(* Export the data to the file “test1.csv” and category “Test1”)}
\]

\[
\text{ExportSGData}[	ext{dataset}, \text{“test1.csv”}, \text{“Test1”}]
\]

\[
\text{(* Import the data from the file *)}
\]

\[
\text{data} = \text{ImportSG}[	ext{“test1.csv”}, \text{“DDD”}];
\]

The corresponding graphics are illustrated in Fig. 5. We give a synthesis of the possible commands in Table 1.

### 2.4. Generating synthetic data and testing cone fitting

For the purposes of testing the cone fitting algorithm a method called GenSGData was developed to generate synthetic conically arranged data. Its first argument is the trend and plunge of the cone axis, the second argument is the apical angle, the third argument specifies the standard deviation around the apical angle and the final argument specifies the number of data to generate. The method works by generating a unit vector \( \mathbf{v} \) randomly oriented in the \( xy \)-plane and then rotating a unit vector parallel to the \( z \)-axis around \( \mathbf{v} \) by an angle selected from a normal distribution with mean equal to the apical angle and the specified standard deviation.

Finally the cone is rotated in parallel with the desired cone axis.

### Table 1

<table>
<thead>
<tr>
<th>Method</th>
<th>Parameters</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ImportSG</td>
<td>Filename</td>
<td>Name of file to be imported</td>
</tr>
<tr>
<td>EqualAreaPlot</td>
<td>Format</td>
<td>Data format, either right hand rule “BHR” or dip/dip direction “DDD”</td>
</tr>
<tr>
<td></td>
<td>Data</td>
<td>Data to be plotted (output from ImportSG)</td>
</tr>
<tr>
<td></td>
<td>Pointrad</td>
<td>Size of points plotted (default value 0.02)</td>
</tr>
<tr>
<td></td>
<td>Igoptions</td>
<td>Specify colour/shape of each dataset in a list e.g. {Blue, OCircle},{Red, FCircle}</td>
</tr>
<tr>
<td></td>
<td>Legend</td>
<td>True/False display a legend or not</td>
</tr>
<tr>
<td>SimpleEqualAreaPlot</td>
<td>Data</td>
<td>Data to plot e.g. {[350,25],[120,36],[249,22]}</td>
</tr>
<tr>
<td></td>
<td>Type</td>
<td>Either “P” or “L” to specify planar or linear data</td>
</tr>
<tr>
<td></td>
<td>Igoptions</td>
<td>Size of points plotted (default value 0.02)</td>
</tr>
<tr>
<td></td>
<td>Labels</td>
<td>An optional ordered list of labels to be placed near each point</td>
</tr>
<tr>
<td>AnalyseSGData</td>
<td>Data</td>
<td>“T” for textual output and “G” for graphical output, default value “T”</td>
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<td>Goptdata</td>
<td>Specify colour/shape of the plotted points e.g. {Blue, OCircle}</td>
</tr>
<tr>
<td></td>
<td>Gopteig</td>
<td>Specify colour/shape of the eigenvector directions e.g. {Blue, OCircle}</td>
</tr>
<tr>
<td></td>
<td>Arccolor</td>
<td>Specify colour of arcs e.g. Black</td>
</tr>
<tr>
<td>FitConeSG</td>
<td>Data</td>
<td>A single dataset returned from ImportSG</td>
</tr>
<tr>
<td></td>
<td>Out</td>
<td>“T” for textual output and “G” for graphical output, default value “T”</td>
</tr>
<tr>
<td></td>
<td>Goptdata</td>
<td>Specify colour/shape of the plotted points e.g. {Blue, OCircle}</td>
</tr>
<tr>
<td></td>
<td>Gopteig</td>
<td>Specify colour/shape of the cone axis e.g. {Blue, OCircle}</td>
</tr>
<tr>
<td></td>
<td>Arccolor</td>
<td>Specify colour of best fit cone trace e.g. Black</td>
</tr>
<tr>
<td></td>
<td>Eigindex</td>
<td>Specify the index of the eigenvector to use as a seed in the algorithm (1, 2 or 3)</td>
</tr>
<tr>
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<td>Conexaxis</td>
<td>Trend/plunge of the cone axis e.g. {54,60}</td>
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<tr>
<td></td>
<td>Apicalangle</td>
<td>Apical angle of the cone e.g. {30}</td>
</tr>
<tr>
<td></td>
<td>Stddev</td>
<td>Controls the level of dispersion around the apical angle</td>
</tr>
<tr>
<td>ExportSGData</td>
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<td>A dataset created by GenSGData</td>
</tr>
<tr>
<td></td>
<td>File</td>
<td>File in which to store the data</td>
</tr>
<tr>
<td></td>
<td>Category</td>
<td>Specify a category for the data</td>
</tr>
</tbody>
</table>
3. A natural example

One of the possible locations of conical folding is in orogens where a phase of deformation is primarily caused by differential rotation around a vertical axis affecting a population of geological surfaces with a variety of initial orientations (Pastor-Gala´n et al., 2012a) meaning that the orogen shows some degree of curvature in plan view. This plan view curvature is recognized in a large number of ancient and modern orogens (e.g. Weil et al., 2000, 2001; Johnston, 2001; Kaymakci et al., 2003; Weil and Sussman, 2004; Marshak, 2004; Van der Voo, 2004; Rosenbaum and Lister, 2004; Allmendinger et al., 2005; Dupont-Nivet et al., 2005; Johnston and Mazzoli, 2009; Johnston and Gutierrez-Alonso, 2010; Pastor-Galán et al., 2011, 2012b; Pastor-Galán et al., 2013; Rosenbaum et al., 2012; Li et al., 2012; Shaw et al., 2012).

A well known orocline or secondary arc is the Ibero Armorican orocline (Fig. 6), which has been recently defined as a true thick-skinned orocline (Gutiérrez-Alonso et al., 2004; Pastor-Gala´n et al., 2012b), constraining kinematics and deformation timing (Weil et al., 2001; Gutiérrez-Alonso et al., 2012; Pastor-Galán et al., 2011) which contains in its core the ca. 180° (isoclinally) buckled foreland fold-and-thrust belt of the Carboniferous Variscan orogenic belt, known as the Cantabrian orocline. This curved sector of the orogenic belt is characterized by two different fold sets: (1) one runs parallel to the outcrops of the main thrusts and describes a horseshoe shape concave towards the east, and (2) another is radial to the arc (Julivert and Marcos, 2005).
A detailed geometric study of the fold interference patterns in the Cantabrian Arc revealed the conical nature of the folds belonging to the radial set. These conical folds developed with different geometrical characteristics (semiapical angles and axis attitudes) depending on the initial orientation and geometry of the folded surfaces. They are interpreted to result from a vertical axis rotation during oroclinal buckling of the Variscan Belt in NW Iberia (Pastor-Galán et al., 2012a).

Data consisting of 578 strike and dip measurements were collected from bedding surfaces of different rock formations (Fig. 7; see Pastor-Galán et al., 2012a for further information) in the Cantabrian Arc. To obtain the best conical fit, folds that have overturned limbs were projected in the lower hemisphere together with the data from the normal limbs.

The geometric study of the fold interference patterns in the Cantabrian Arc revealed the conical nature of the folds belonging to the radial set (Fig. 7). These conical folds developed with different geometrical characteristics depending on the initial orientation and geometry of the folded surfaces. This conical folding is interpreted to result from a vertical axis rotation during oroclinal buckling of the Variscan Belt in NW Iberia (Pastor-Galán et al., 2012a).

4. Conclusions

Due to the lack of available software adequate to do a proper conical fit, we have developed a Mathematica code implementing the Fisher et al. (1987) pp. 140–143, based on Mardia and Gadsden (1977), for least-squares cone fitting. With this code it is possible to obtain semi-apical angles of the cones, orientation of fold axes and errors. Additionally, it exports the stereographic projection as vector graphics format (.pdf files) facilitating the edition of figures to be published.

We have tested the code firstly with synthetic datasets in order to notice the robustness of the method and code. After that, we tested the method and code with a complex geometric natural example from NW Iberia. Both tests indicate that the method used is confident and the robustness of the code to obtain the best conical fit using stereographic projection.

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Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at http://dx.doi.org/10.1016/j.cageo.2013.01.005.

References


